

Recent Developments on Advanced Macromodeling by Politecnico di Torino

Tommaso Bradde, Marco De Stefano, Alessandro Zanco, Stefano Grivet-Talocia

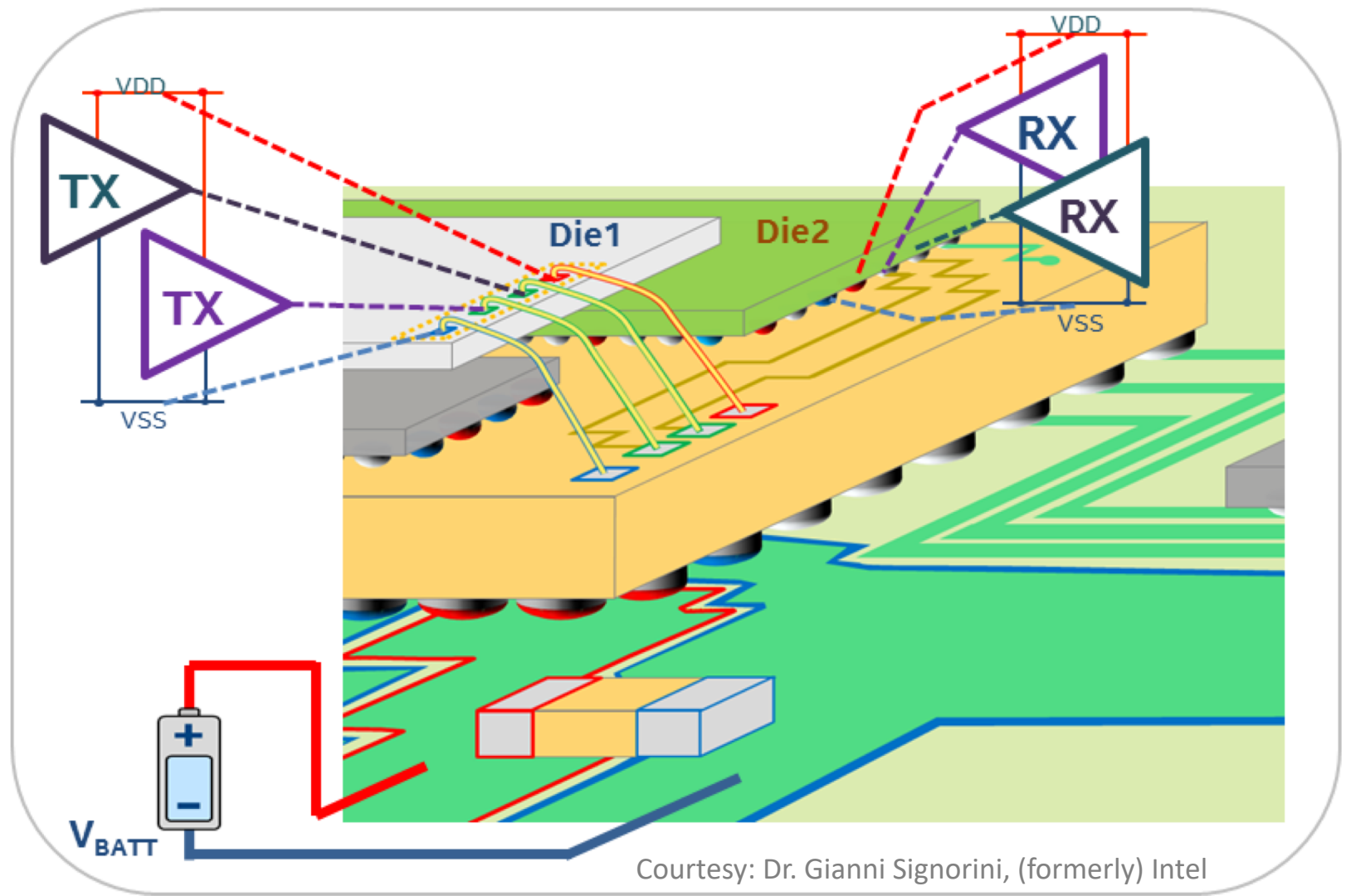
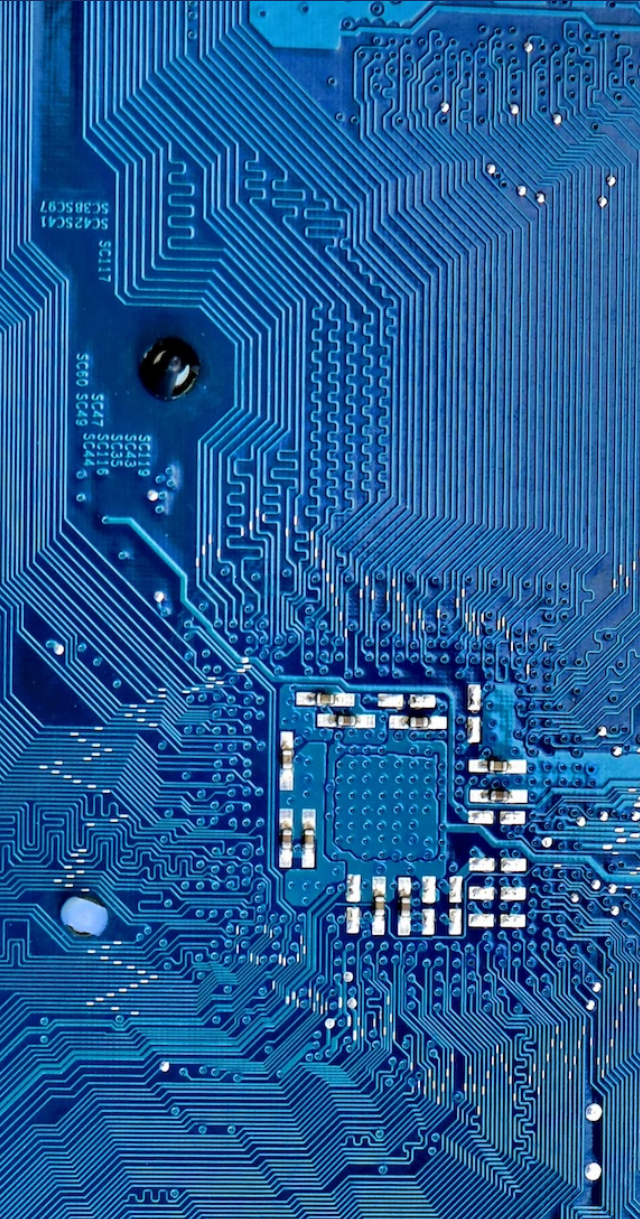
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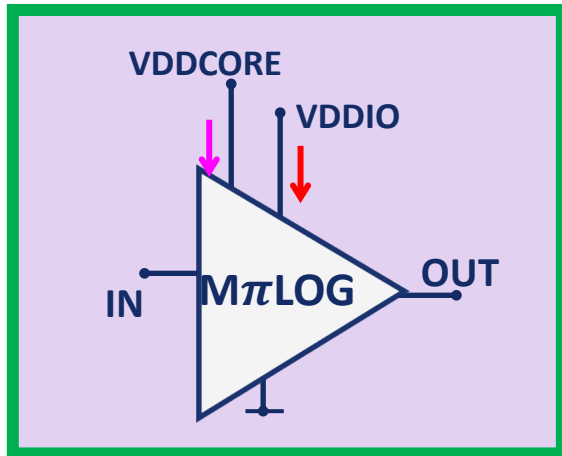


**POLITECNICO
DI TORINO**

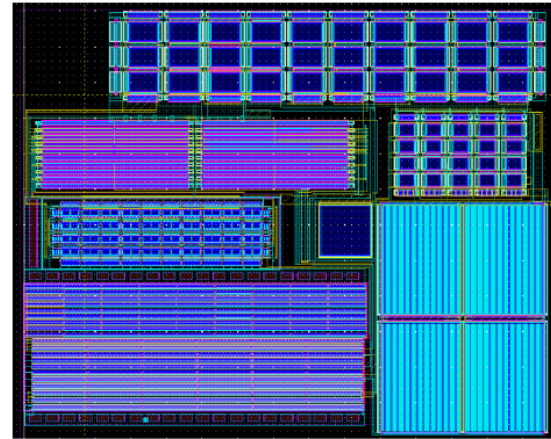




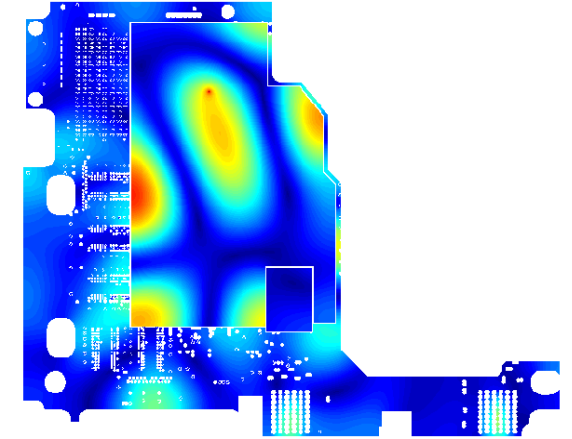
Behavioral models: used extensively and successfully to approximate...



I/O Buffers



Analog Devices



Passive Structures

Many different modeling techniques (such as IBIS standards) are available

The most appropriate approach is application-dependent

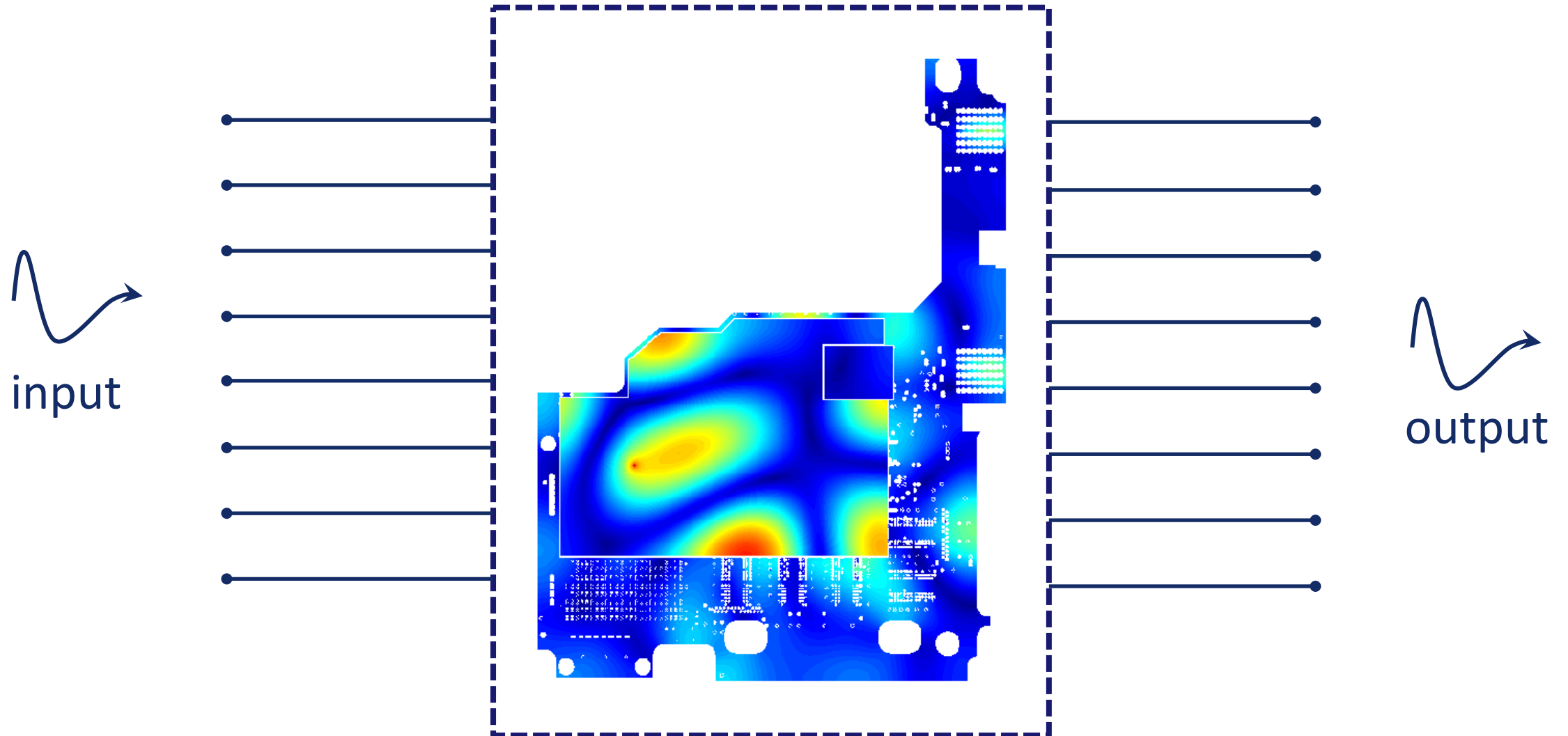
We will focus here on passive structures and partially on analog devices

Behavioral models are intrinsically:

- **Simplified** and accurate descriptions
- Very general and **design-independent**
 - black-box: do not unveil details of the underlying design

Additional desirable features:

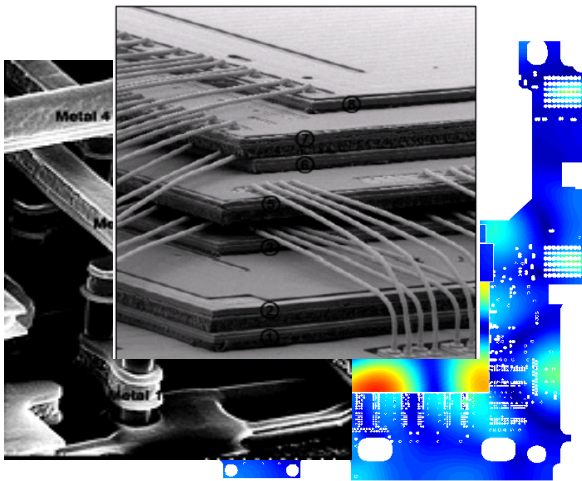
- **Compliance** with spice-like circuit solvers or other common **simulation environments**
- **Compliance** with **fundamental properties** of the reference system (e.g. stability and passivity)
- Generated automatically by non-expert users



Courtesy Prof. Swaminathan, GA Tech

Passive structures dynamics are properly described by linear ODEs or PDEs

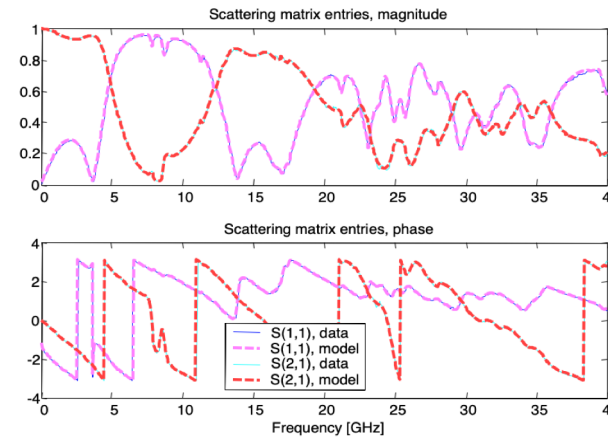
Geometry, materials



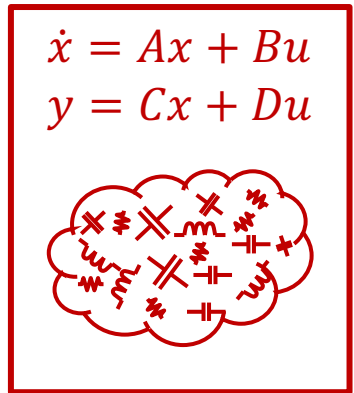
Extraction
EM simulation
Ckt simulation



Scattering data $\hat{S}_k = \hat{S}(j\omega_k)$



Macromodel



LTI systems are best represented by rational transfer functions

Rational fitting
Passivity enforcement

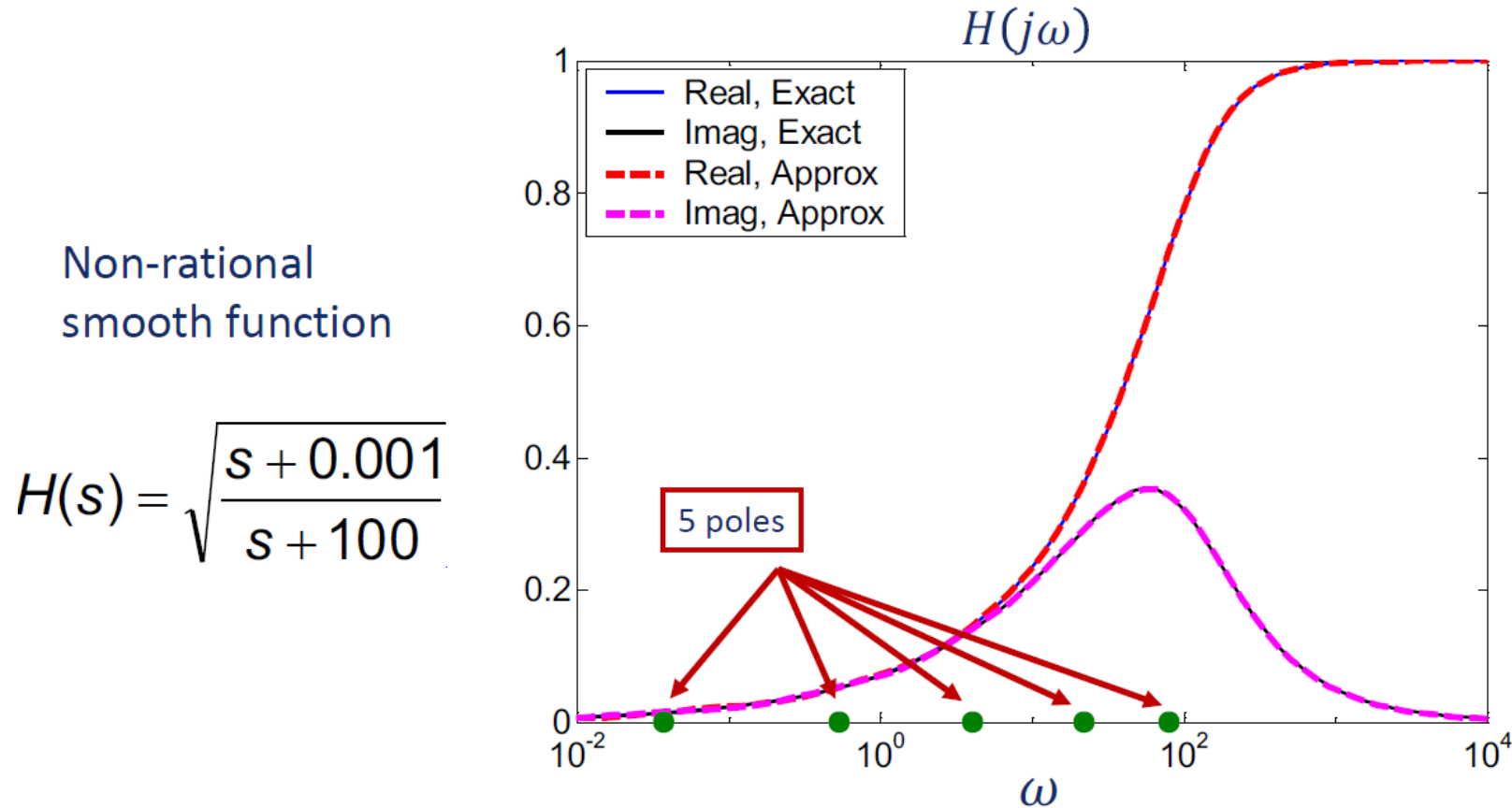


$$S(s) = \sum_{n=1}^N \frac{R_n}{s - p_n} + S_\infty$$

Realization or synthesis



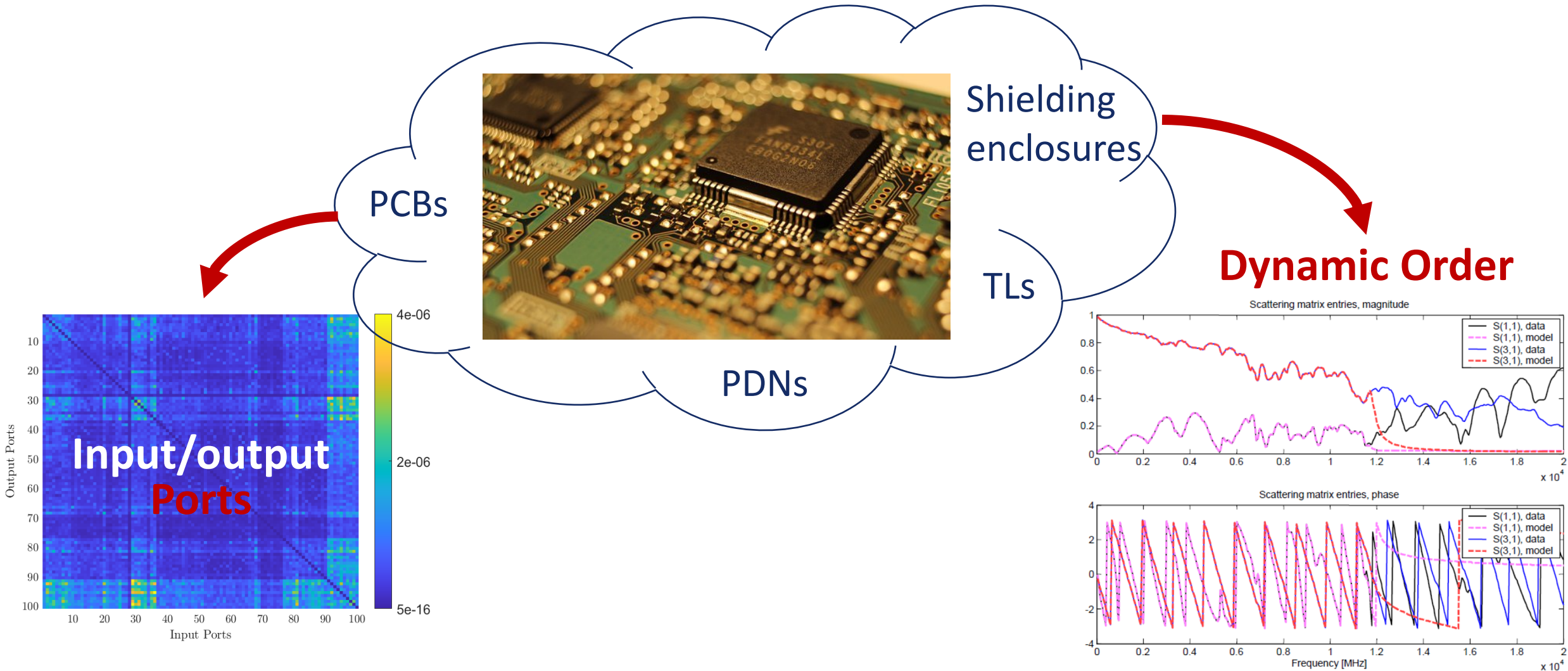
The approximations are topology-free and can potentially reproduce a variety of behaviors typical of distributed-parameter systems

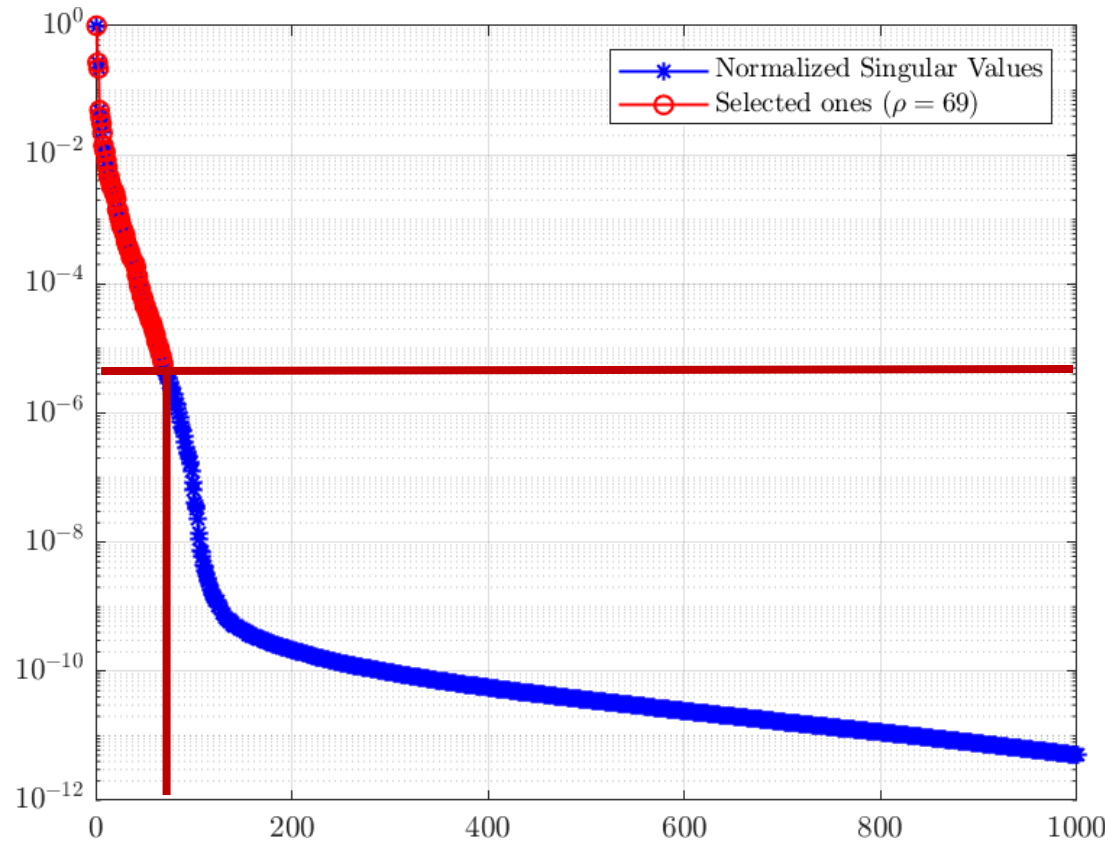


- Recent advancements on macromodeling by Politecnico di Torino
 - Macromodeling of large-scale systems (hundreds of I/O ports)
 - Speaker: Marco De Stefano, PhD candidate
 - Compression strategies
 - Fast passivity verification and enforcement
 - Parameterized (multivariate) macromodels
 - Speaker: Alessandro Zanco, PhD candidate
 - Model structure and enhanced scalability (Radial Basis Functions – RBF)
 - Stability enforcement
 - Small-signal modeling of (nonlinear) analog circuit blocks
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 - Theoretical assessment of dissipativity

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Large-Scale LTI Systems



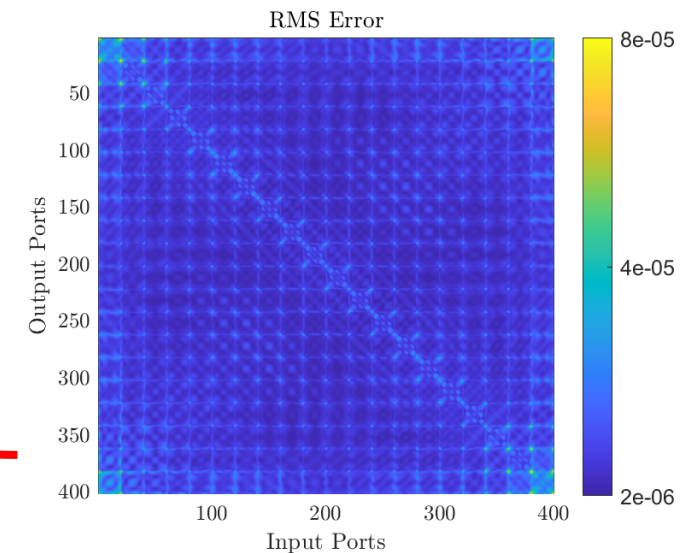
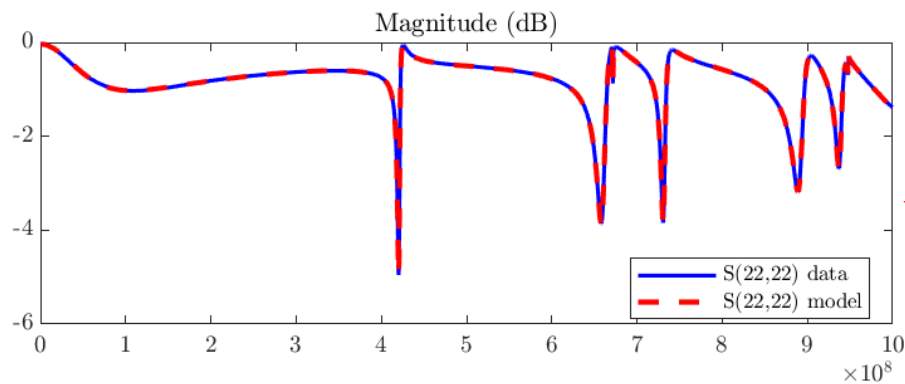


For structures with **many electrical ports**, the behavior can be recovered as a linear combination of a **reduced number** of case-dependent basis functions obtained from a **data-compression technique** (e.g. truncated SVD)

69 out of 160000 !!!

Surrogate Macromodeling → Data Compression Technique + Vector Fitting

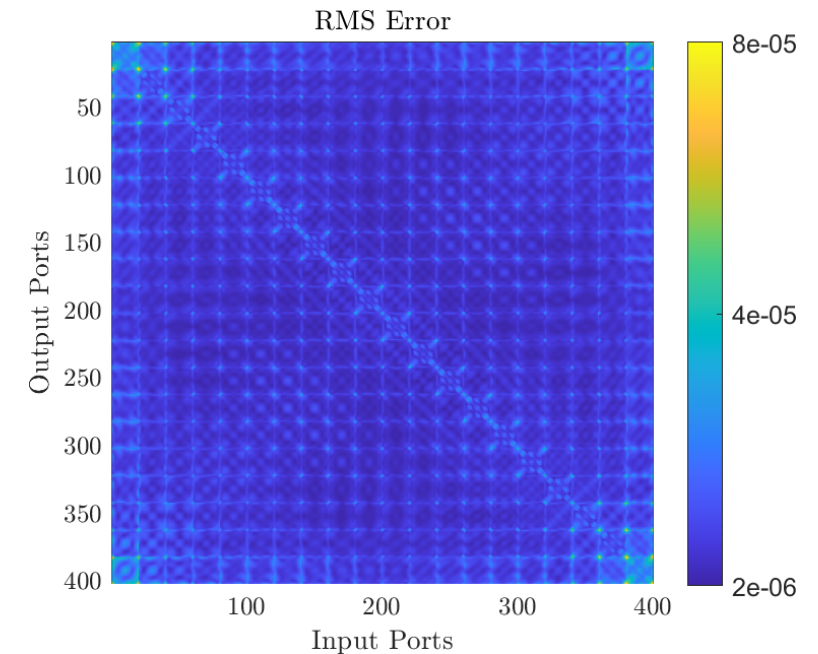
- + Accurate and Fast
- + Data compression based on Singular Value Decomposition (SVD)
- + Robust and reliable: full control over accuracy



Accuracy **OK**, Stability **OK**, Passivity **???**

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- Passivity check based on a **Hamiltonian matrix eigenvalues** computation is the state-of-the-art
- Such technique becomes **infeasible** when the model **complexity grows**, in terms of
 - P: Ports
 - N: Number of Poles
- **Computational cost scales as $O((kPN)^3)$**



64 GB of RAM necessary to check passivity of 400-port, 90-pole model

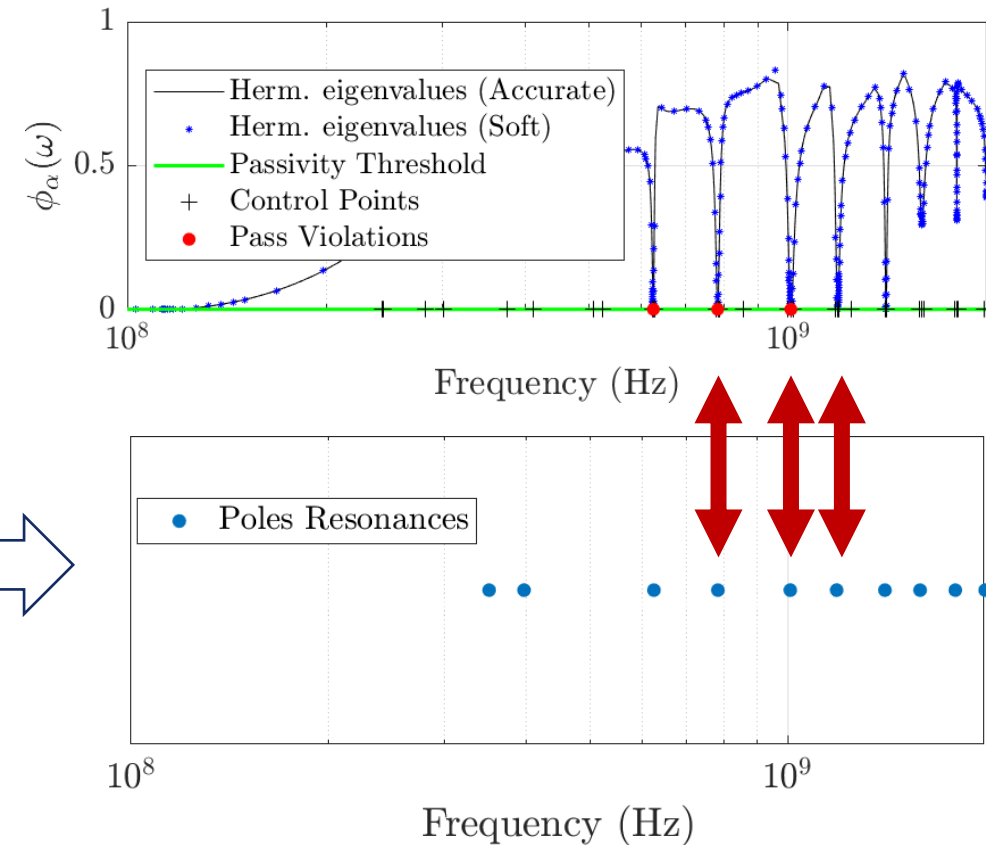
A new procedure to address large-size macromodels is **required**
→ adaptive sampling in the frequency domain may be sufficient...

Adaptive-sampling-based passivity checking scheme developed to overcome the complexity of Hamiltonian checks

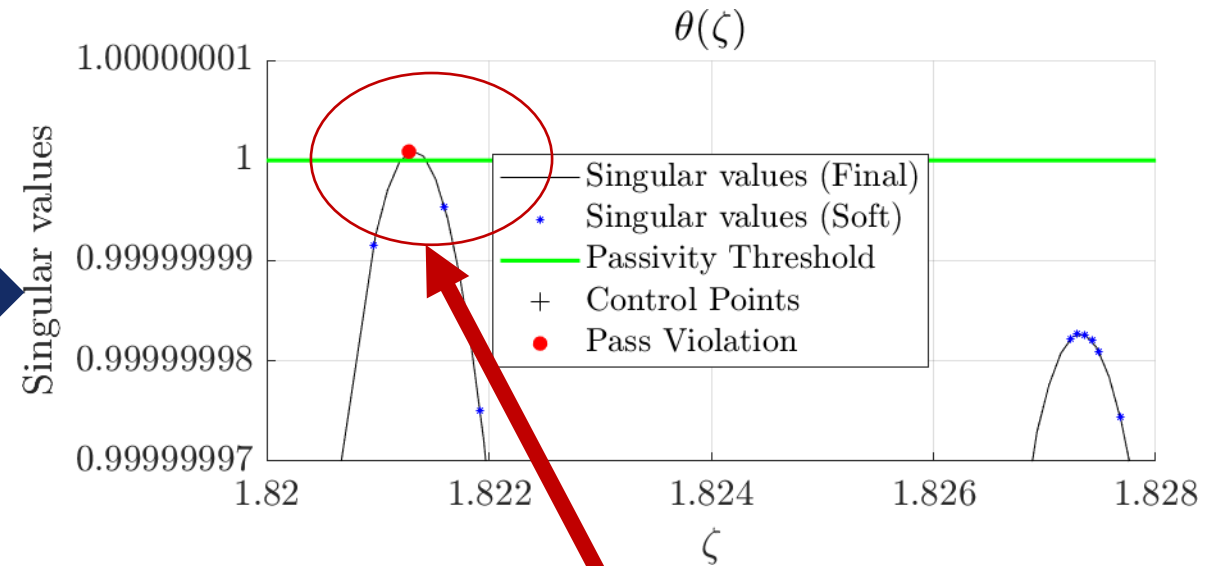
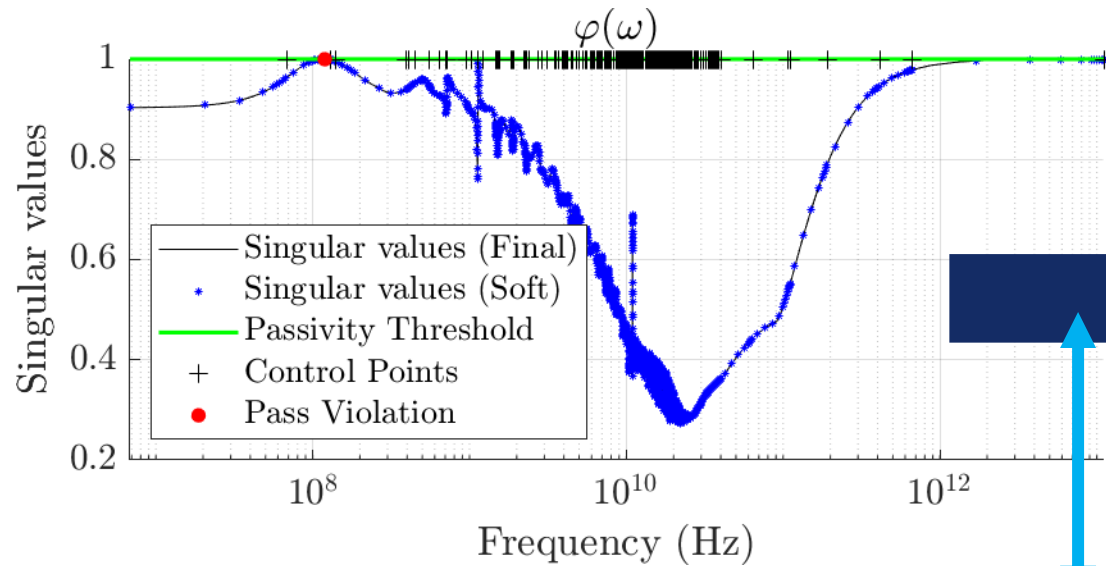
Based on a **2-stage** approach

- 1. Pole-based adaptive frequency warping**
- 2. A passivity-driven tree-search divide-and-conquer strategy**

Fast variations of eigenvalues (or singular values) trajectories are mostly induced by the model **poles resonances**



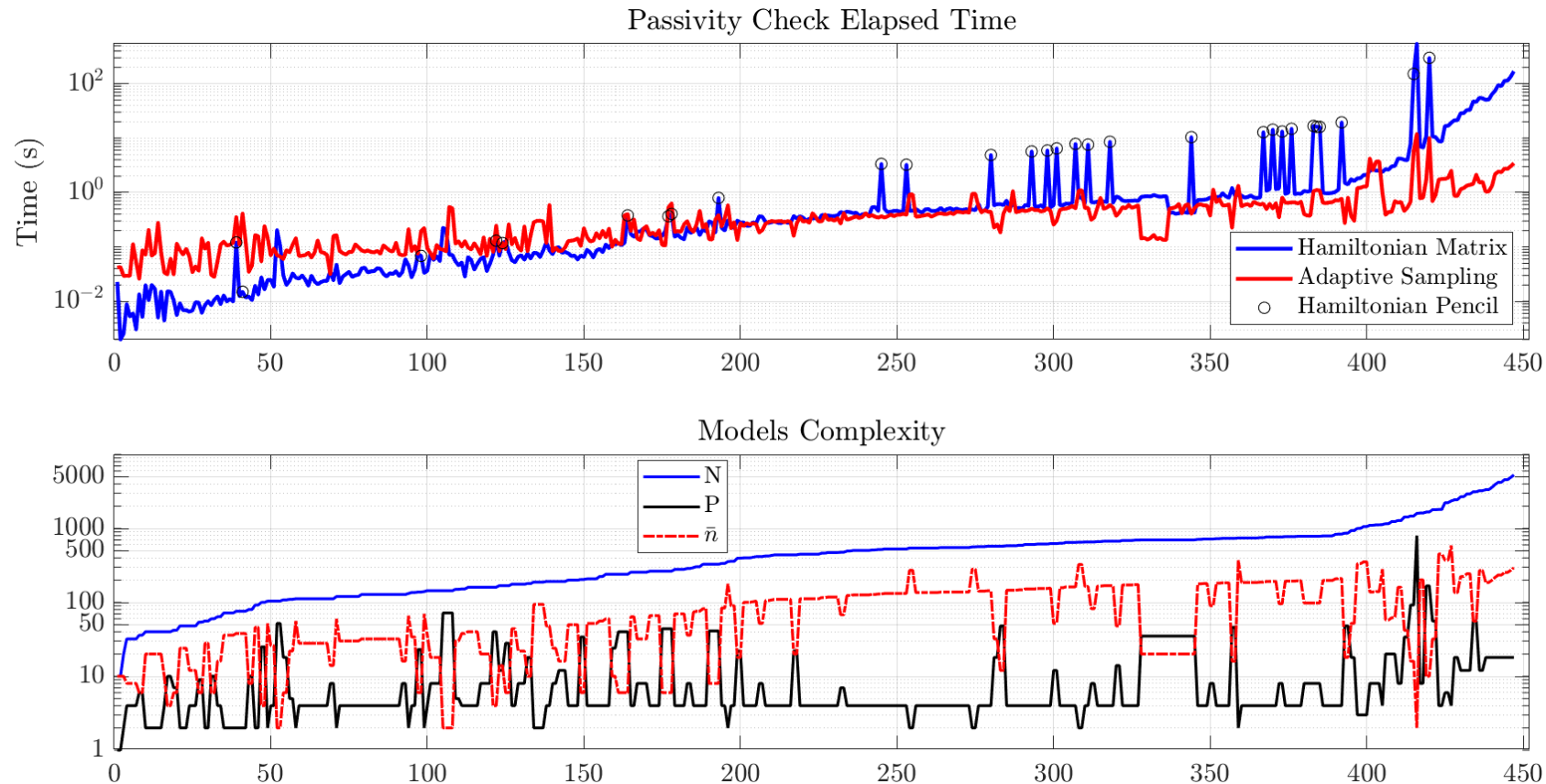
The result is a **fast and reliable** strategy for the **passivity characterization** of **large-scale macromodels**



Frequency Warping = Change of variable
 $\zeta = \mathcal{W}(f)$

Very small passivity violations can be effectively detected!

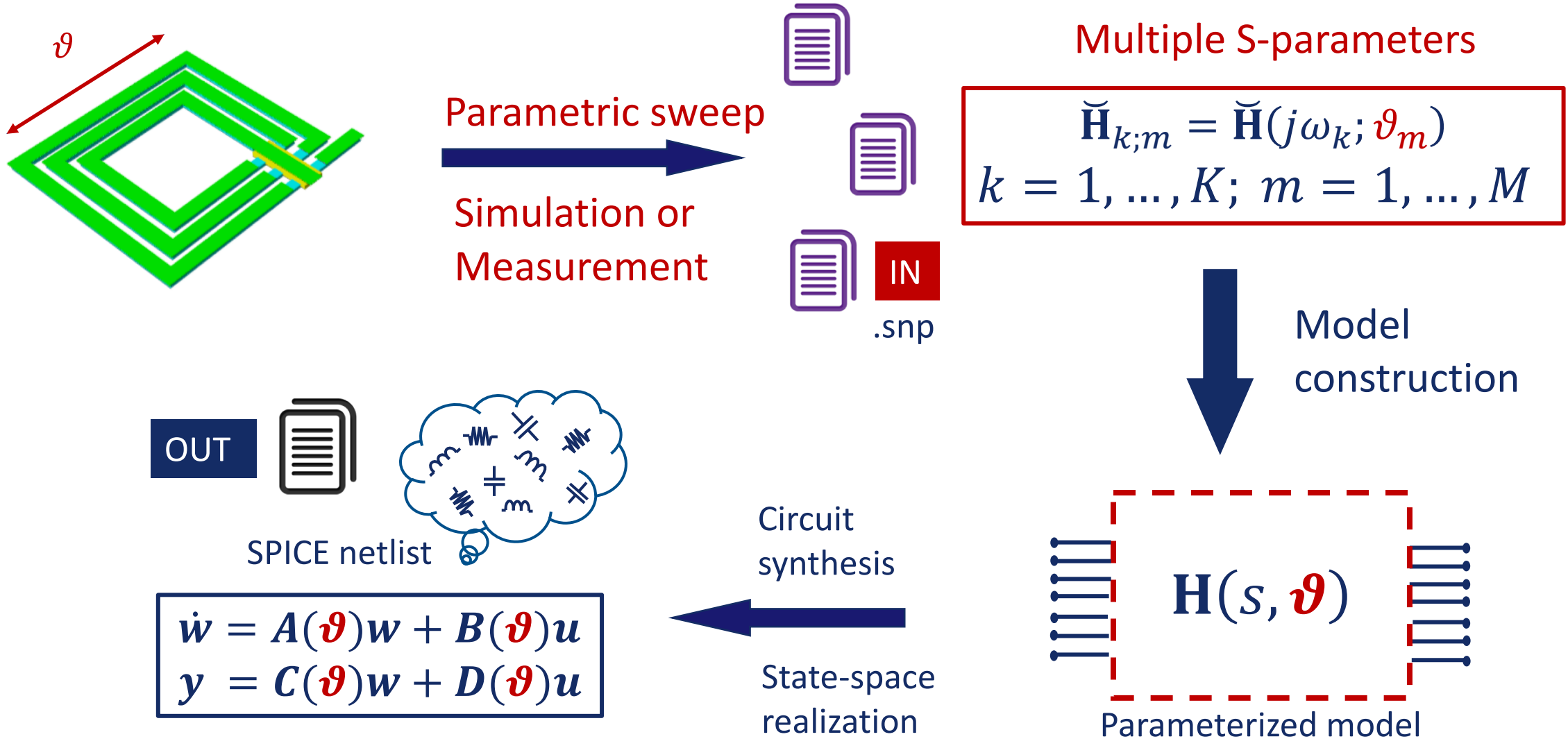
Massive testing campaign to assess the algorithm reliability



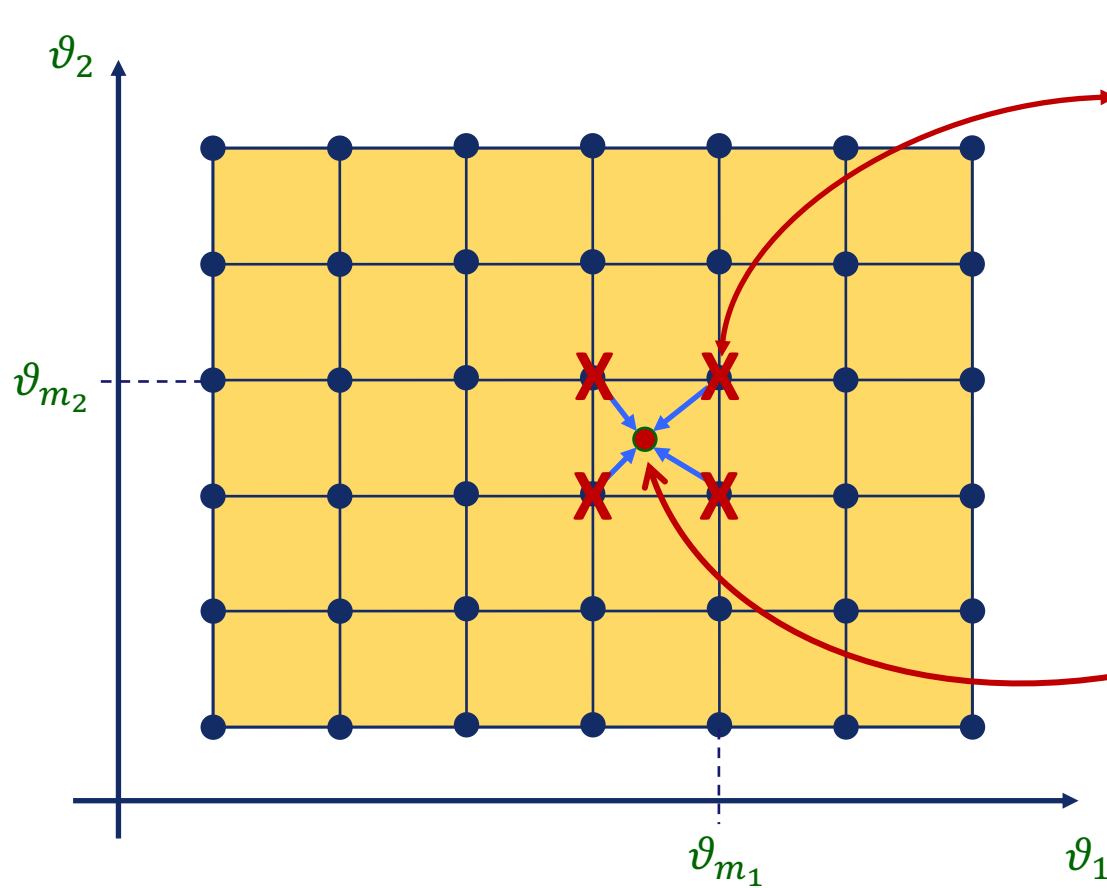
- + All examples run on **8GB of RAM** laptop (**64GB** are required for the **Hamiltonian Check**)
- + large size cases **speed-up from 10 to 100X**
- + small and medium size performances are comparable

M. De Stefano, S. Grivet-Talocia, W. Torben, C. Yang, C. Schuster, "A Multistage Adaptive Sampling Scheme for Passivity Characterization of Large-Scale Macromodels", IEEE Trans. CPMT, vol. 11, no. 3, pp. 471–484, March 2021

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Approach #1: interpolate independent non-parametric “root” macromodels



$$\mathbf{H}(s, \boldsymbol{\vartheta}_m) = \sum_{n=1}^N \frac{\mathbf{R}_n^m}{s - p_n^m} + \mathbf{H}_\infty^m$$

“Root” models in pole-residue form (each with individual poles and residues)

$$\mathbf{H}(s, \boldsymbol{\vartheta})$$

Obtained by **interpolating** the closest “root” models

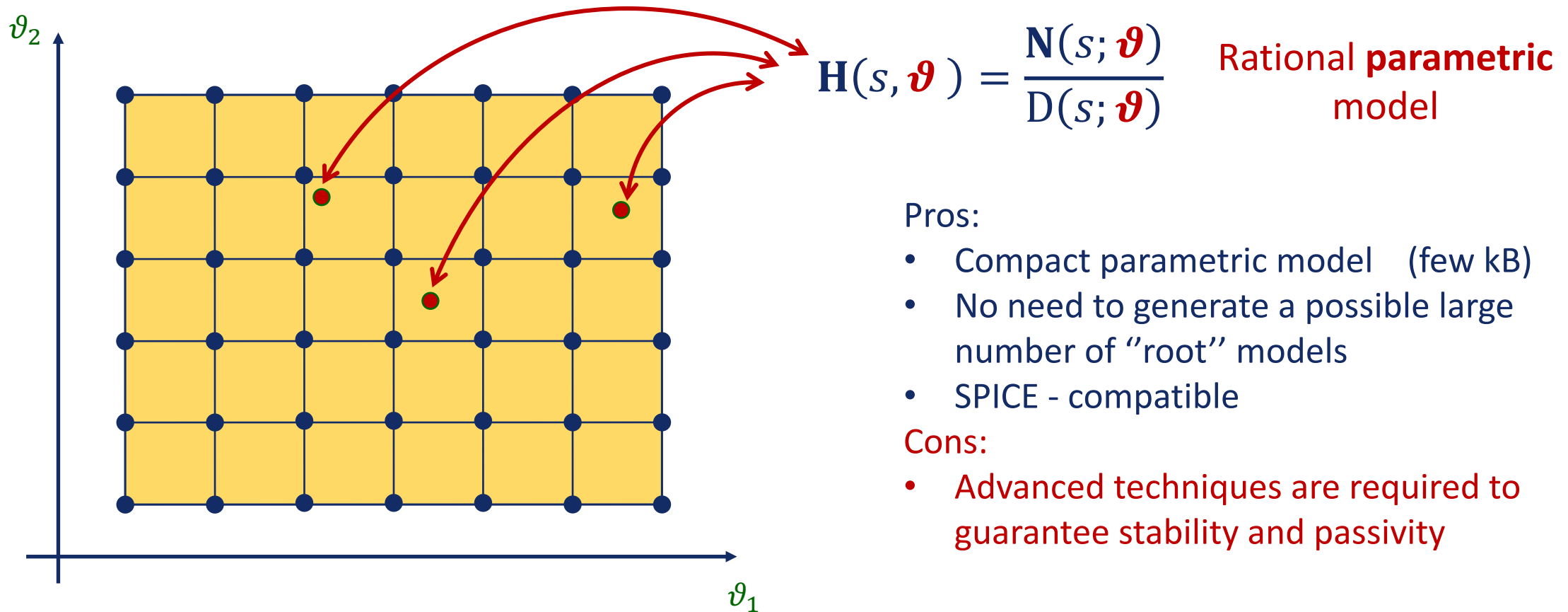
Pros:

- Very simple scheme
- Interpolation schemes exist that guarantee passivity

Cons:

- Model is fully defined only by including a large set of “root” macromodels
- Poles are usually many more than required

Approach #2: embed in closed the parameter variability in the model



Pros:

- Compact parametric model (few kB)
- No need to generate a possible large number of “root” models
- SPICE - compatible

Cons:

- Advanced techniques are required to guarantee stability and passivity

Rational model structure

$$\mathbf{H}(s; \boldsymbol{\vartheta}) = \frac{\mathbf{N}(s; \boldsymbol{\vartheta})}{\mathbf{D}(s; \boldsymbol{\vartheta})} = \frac{\sum_n \sum_\ell \mathbf{R}_{n,\ell} \xi_\ell(\boldsymbol{\vartheta}) \varphi_n(s)}{\sum_n \sum_\ell r_{n,\ell} \xi_\ell(\boldsymbol{\vartheta}) \varphi_n(s)}$$

Partial Fractions $\varphi_n(s) : \frac{1}{s - q_n}$

Parameter basis function $\xi_\ell(\boldsymbol{\vartheta}) :$

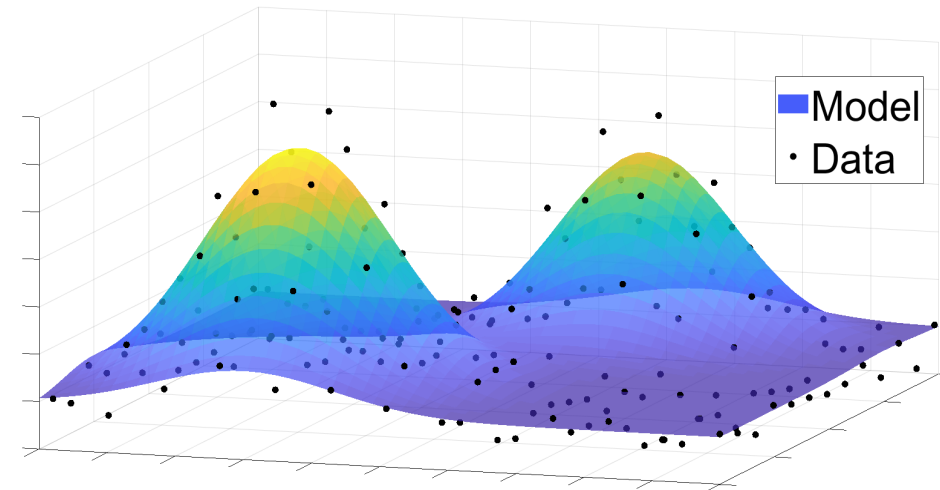
High-dimensional **kernel (RBF)** expansion

Gaussian kernel $\xi_\ell(\boldsymbol{\vartheta}) = e^{-\varepsilon \|\boldsymbol{\vartheta} - \boldsymbol{\vartheta}_\ell\|^2}$

To be estimated

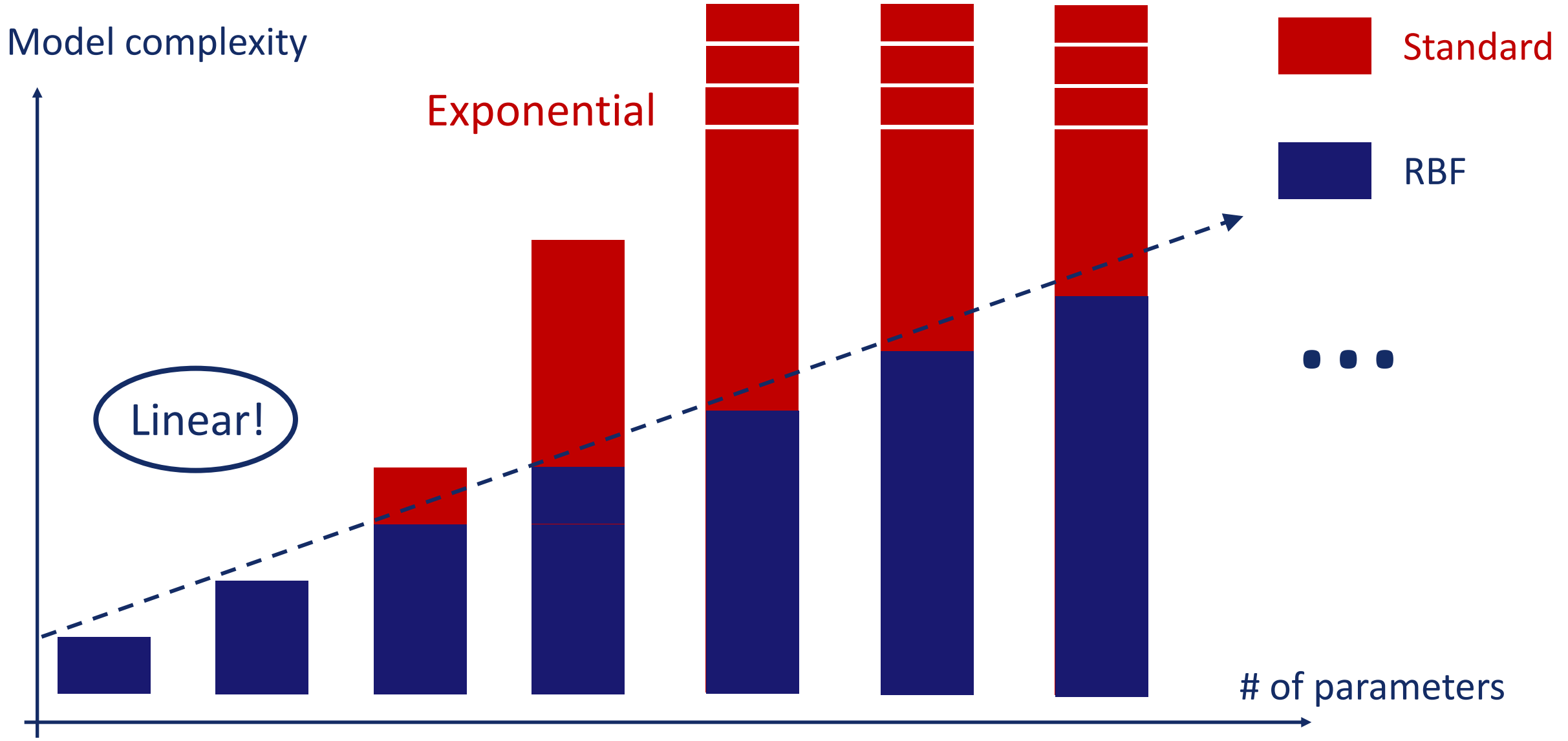


$$\frac{\mathbf{N}(s; \boldsymbol{\vartheta})}{\mathbf{D}(s; \boldsymbol{\vartheta})} \approx \check{\mathbf{H}}(j\omega_k; \boldsymbol{\vartheta}_m)$$



PRO:

Good scalability in high-dimensions



The model $\mathbf{H}(s; \boldsymbol{\vartheta})$ depends upon some free **hyper-parameters**, whose number:

STANDARD

Scales exponentially

RBF

Fixed!!!

Gaussian kernel

$$\xi_{\ell}(\boldsymbol{\vartheta}) = e^{-\varepsilon \|\boldsymbol{\vartheta} - \boldsymbol{\vartheta}_{\ell}\|^2}$$

Shape parameter

of RBFs
RBF's centers

There exists techniques to optimize these hyper-parameters for model compactness and accuracy

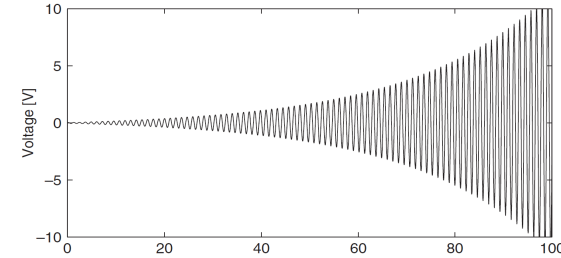
A. Zanco and S. Grivet-Talocia, "Hyperparameter determination in multivariate macromodeling based on radial basis functions," in Proc. IEEE 29th Conf. Electr. Perform. Electron. Packag. Syst. (EPEPS), San Jose, CA, USA, Oct. 2020, pp. 1–3.

A. Zanco, S. Grivet-Talocia, "A mesh-free adaptive parametric macromodeling strategy with guaranteed stability," in Proc. International Symposium on Electromagnetic Compatibility 2020 - EMC Europe 2020, Rome, Italy, Sept. 2020, pp. 1-6.

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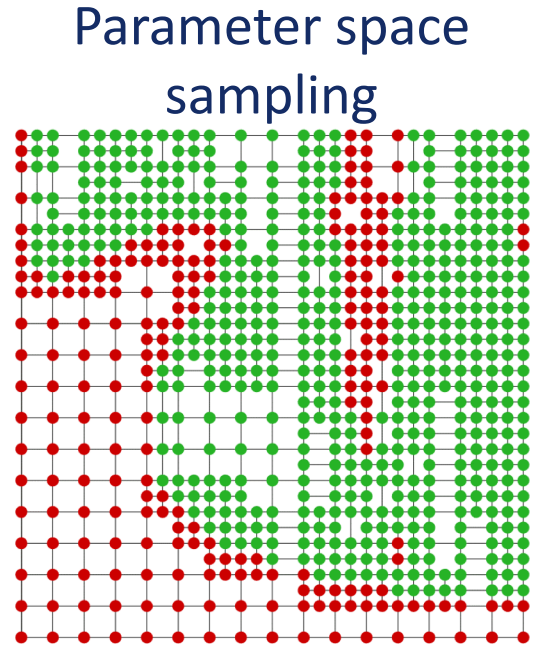
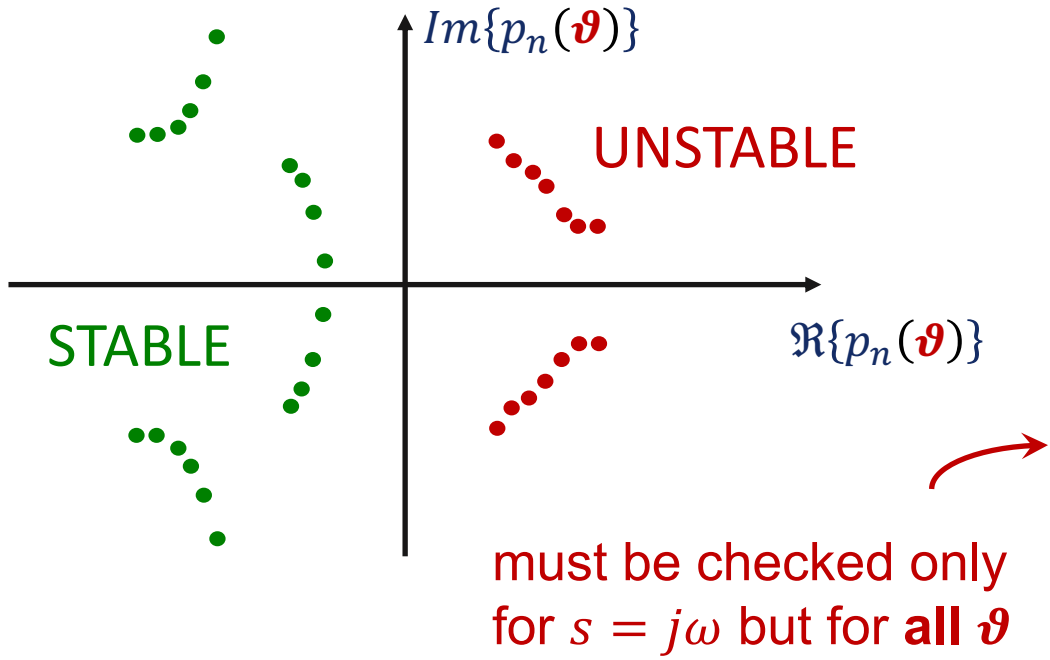
Implicit poles parameterization
NO CONTROL ON POLES LOCATIONS!



For uniform stability
 $\Re\{D(s; \boldsymbol{\vartheta})\} > 0, \forall s, \boldsymbol{\vartheta}$

↓

$\Re\{p_n(\boldsymbol{\vartheta})\} < 0, \text{ for all } \boldsymbol{\vartheta}$



Stefano Grivet-Talocia, Riccardo Trincherò. "Behavioral, parameterized, and broadband modeling of wired interconnects with internal discontinuities." *IEEE Transactions on Electromagnetic Compatibility* 60.1 (2017): 77-85.

... but, with positive-definite kernels ...

$$\Re\{D(s; \boldsymbol{\vartheta})\} = \Re\left\{\sum_n \sum_l r_{n,l} \xi_l(\boldsymbol{\vartheta}) \varphi_n(s)\right\} > 0$$



$$\Re\left\{\sum_n \sum_l r_{n,l} \varphi_n(s)\right\} > 0$$

$$\begin{cases} r_{n,l} > 0 & \text{for real poles } q_n \\ -\alpha_n r'_{n,l} \pm \beta_n r''_{n,l} > 0 & \text{for complex poles } \alpha_n \pm j\beta_n \end{cases}$$

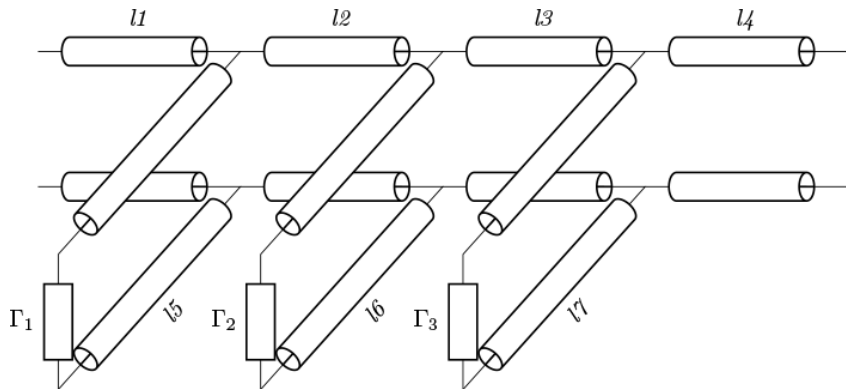
$$\varphi_n(s) : \frac{1}{s - q_n}$$

No parameter-space sampling!

Few constraints in few variables!

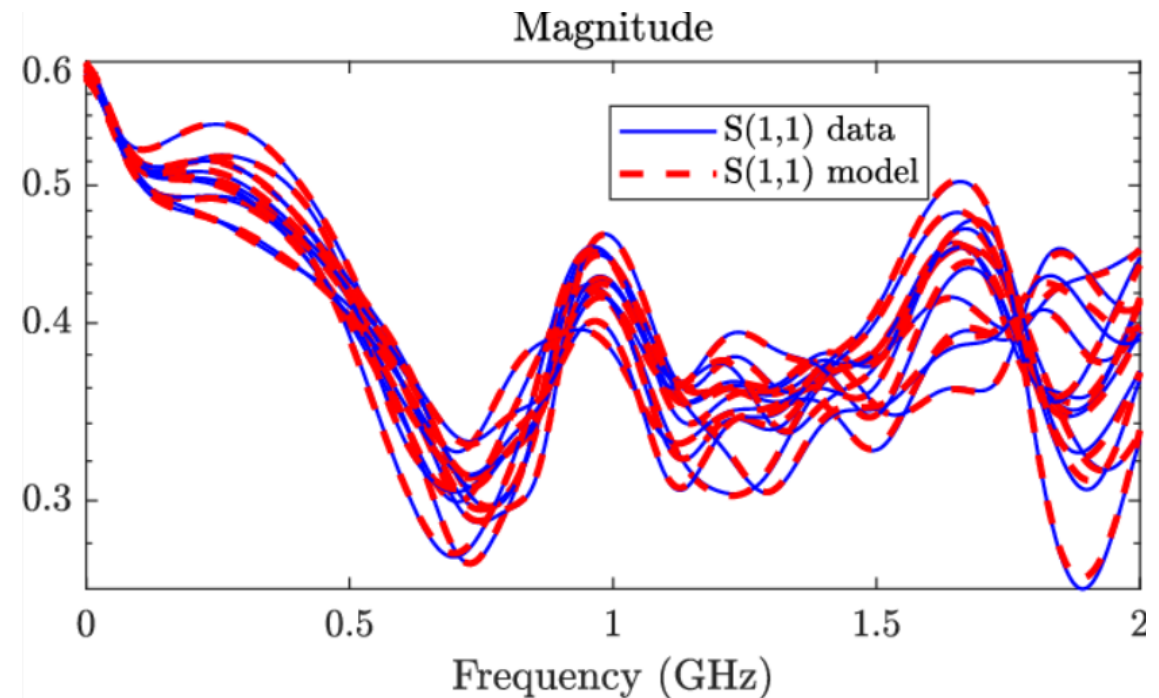
Analytic stability constraints!

A parameterized microstrip transmission line



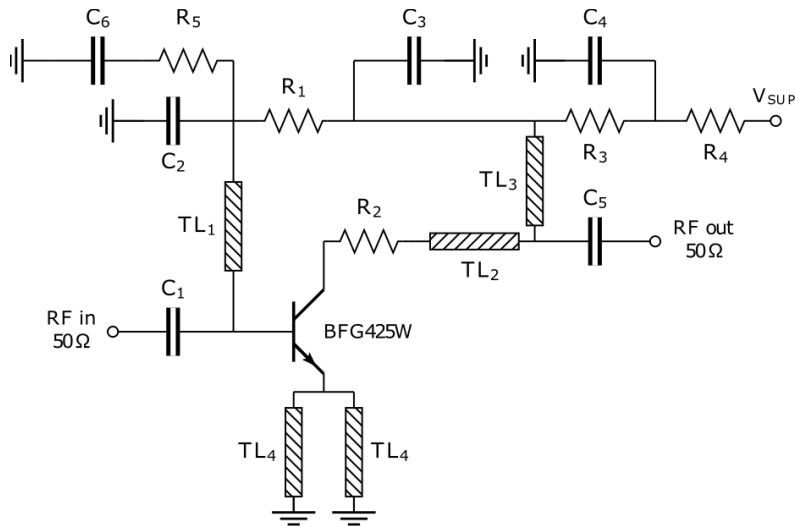
10-independent parameters

- Inner lines length
- Stubs length
- Load resistances
- Substrate electrical parameters

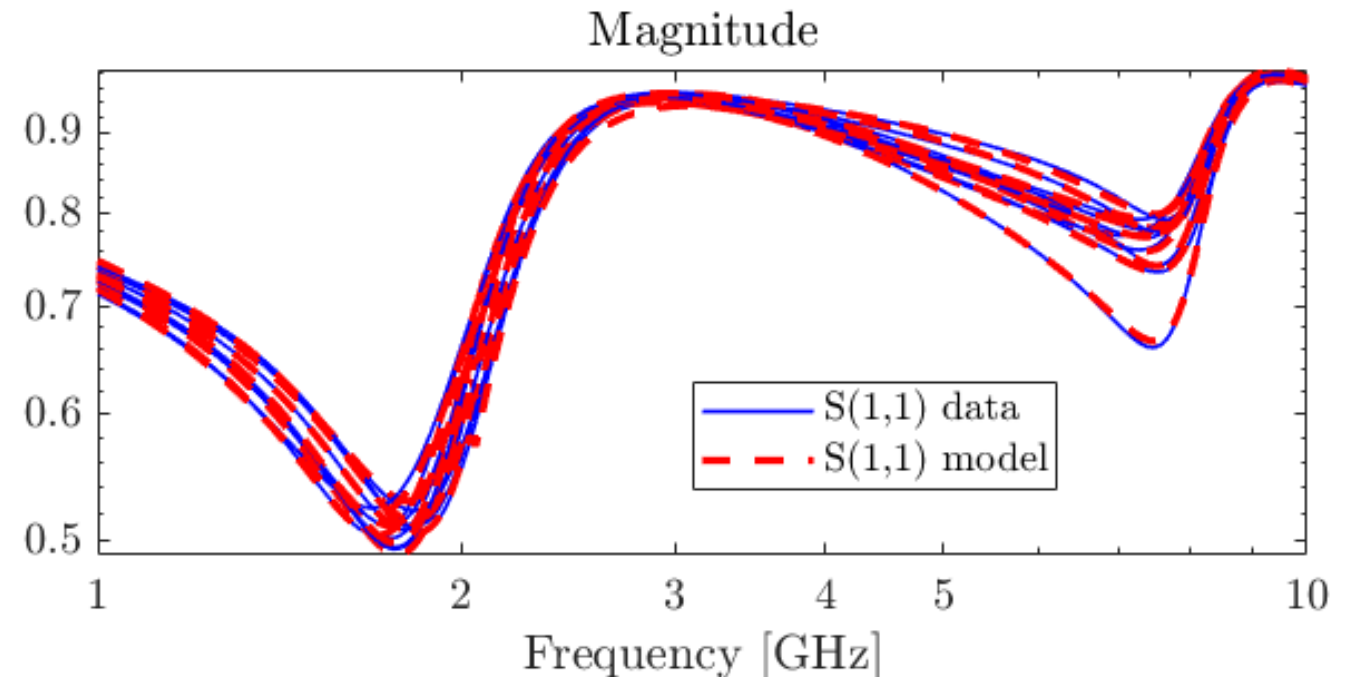


It required 14 minutes to extract a **STABLE** model, with accuracy 11×10^{-3}

Low Noise Amplifier



Automatic generation of a **STABLE** parameterized model: **6 minutes!**



Model vs Data error: $9.2 \cdot 10^{-3}$

#	Parameter ϑ_i	$\vartheta_{i,\min}$	$\vartheta_{i,\max}$
1	L_b (nH)	0.88	1.32
2	L_c (nH)	0.88	1.32
3	L_e (nH)	0.20	0.30
4	C_{cb} (pF)	0.0016	0.0024
5	C_{be} (pF)	0.064	0.096
6	C_{ce} (pF)	0.064	0.096
7	h (mm)	0.45	0.55
8	t_k (μm)	1.8	2.2
9	$w_{1,2,3}$ (mm)	0.225	0.275
10	w_4 (mm)	0.72	0.88

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Nonlinear equations

$$\dot{w} = F(w, u)$$

$$y = G(w, u)$$

Small signal analysis



Linearization around the operating point

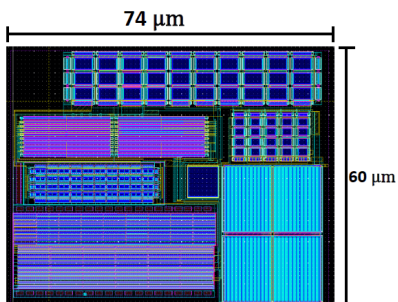
Local model

$$\dot{w} = Aw + Bu$$

$$y = Cw + Du$$

PROBLEM: post-layout circuit equations are unavailable (hidden)

SOLUTION: data driven modeling approach based on AC analysis



Rational Approximation
(Vector Fitting)

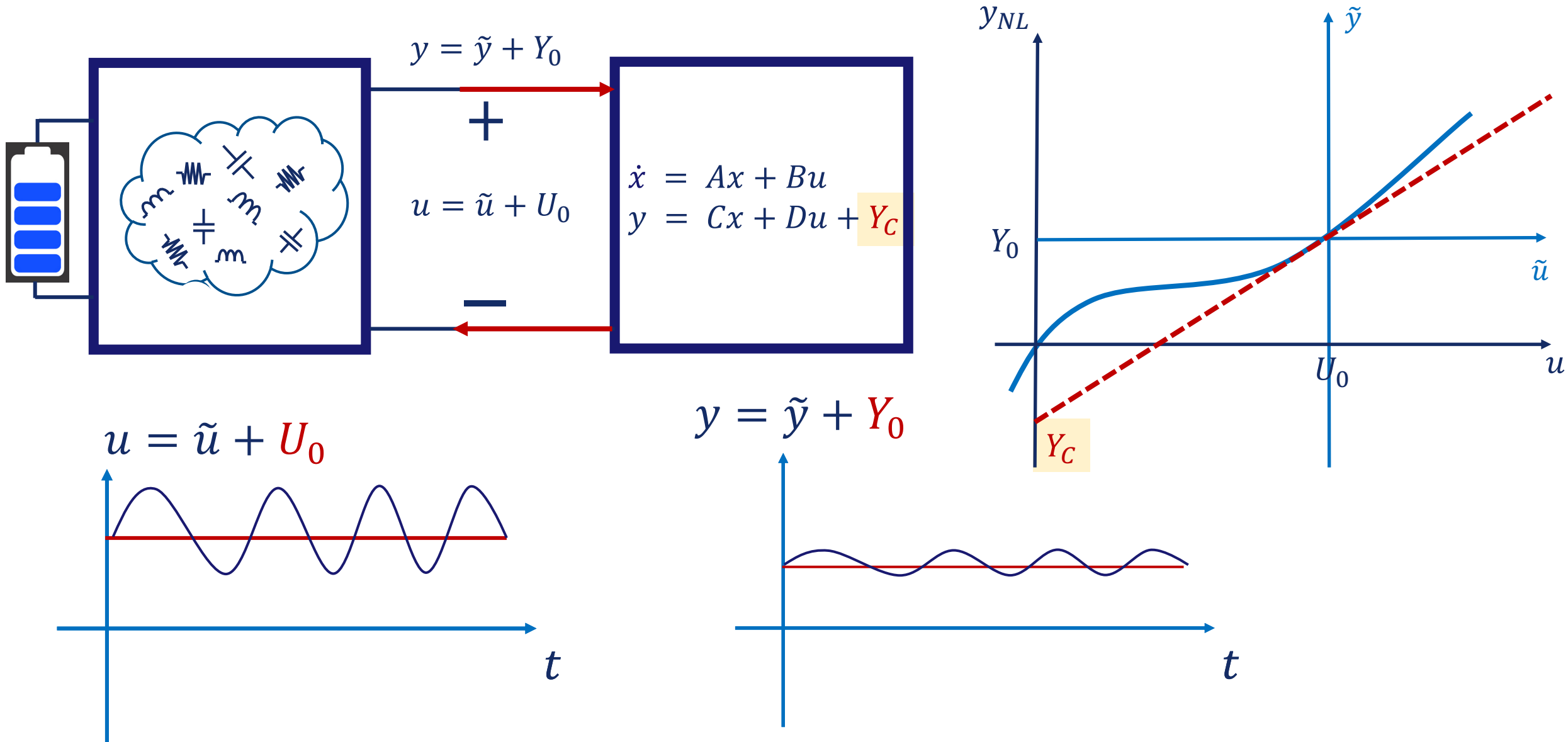
Reduced order

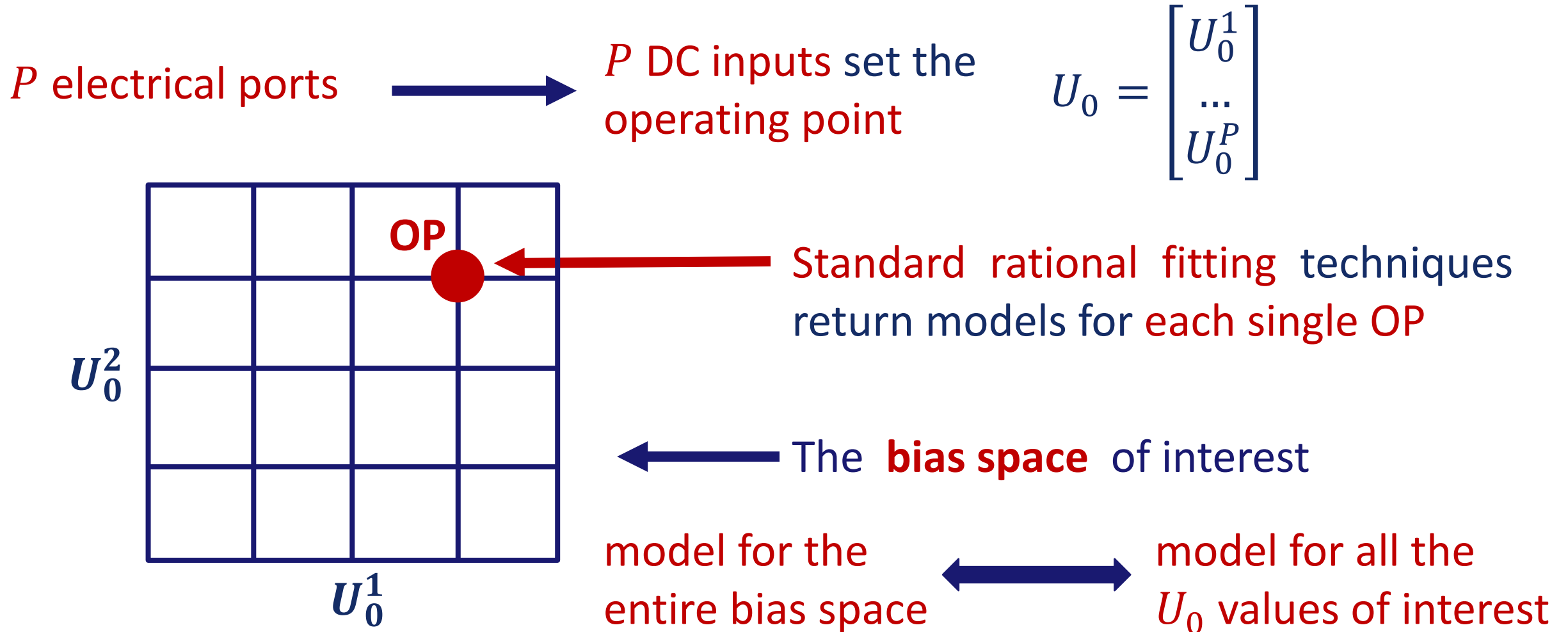
local model

$$\dot{x} = Ax + Bu$$

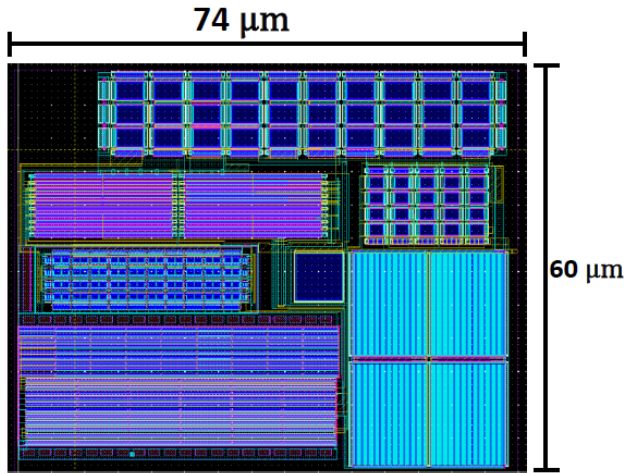
$$y = Cx + Du$$

Affine linearized models of NL analog blocks





Bradde, T., et al. Enabling fast power integrity transient analysis through parameterized small-signal macromodels. In: 2019 International Symposium on Electromagnetic Compatibility-EMC EUROPE. IEEE, 2019. p. 759-764.



Parametric sweep



Simulation or
Measurement



IN

Frequency response data

$$\check{H}_{k;m} = \check{H}(j\omega_k; \vartheta_m)$$

$$k = 1, \dots, K; m = 1, \dots, M$$

Multivariate
Rational
Fitting

Stability

OUT



SPICE netlist

$$\dot{x} = A(\vartheta)x + B(\vartheta)u$$

$$y = C(\vartheta)x + D(\vartheta)u + Y_C(\vartheta)$$

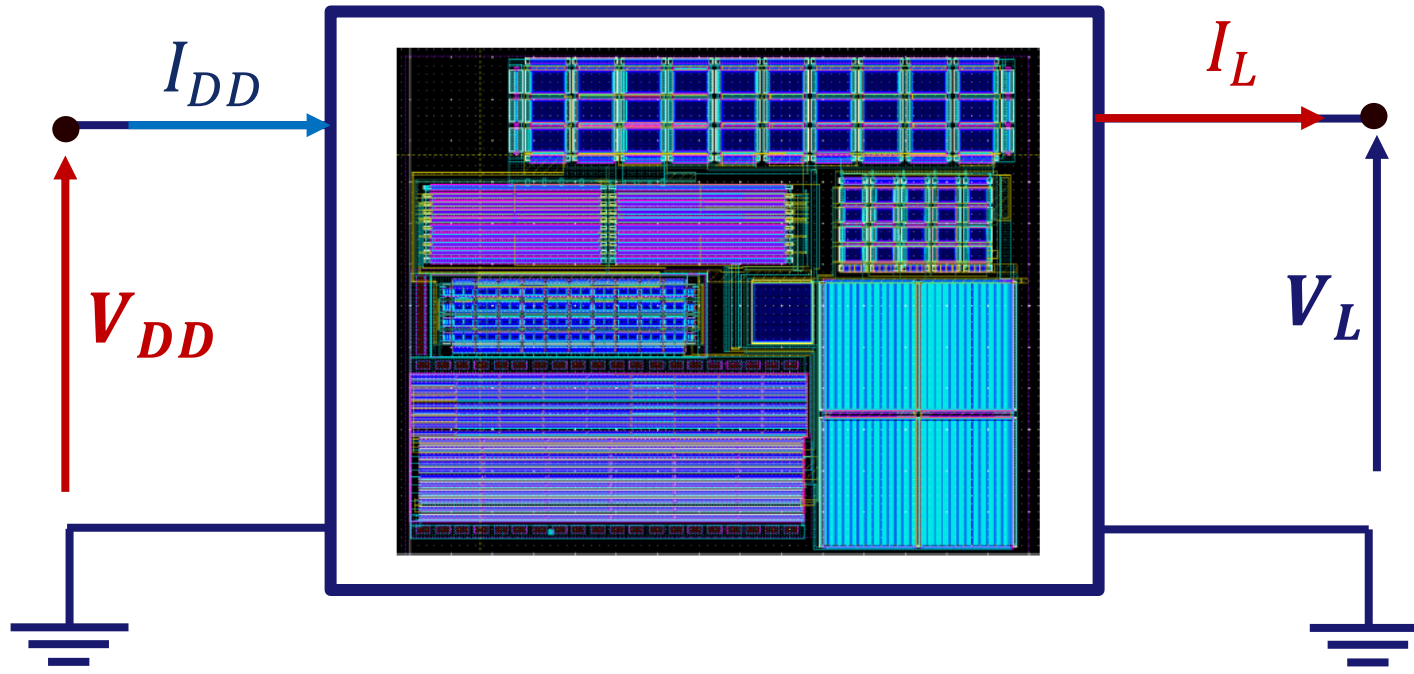
State-space realization



Circuit synthesis

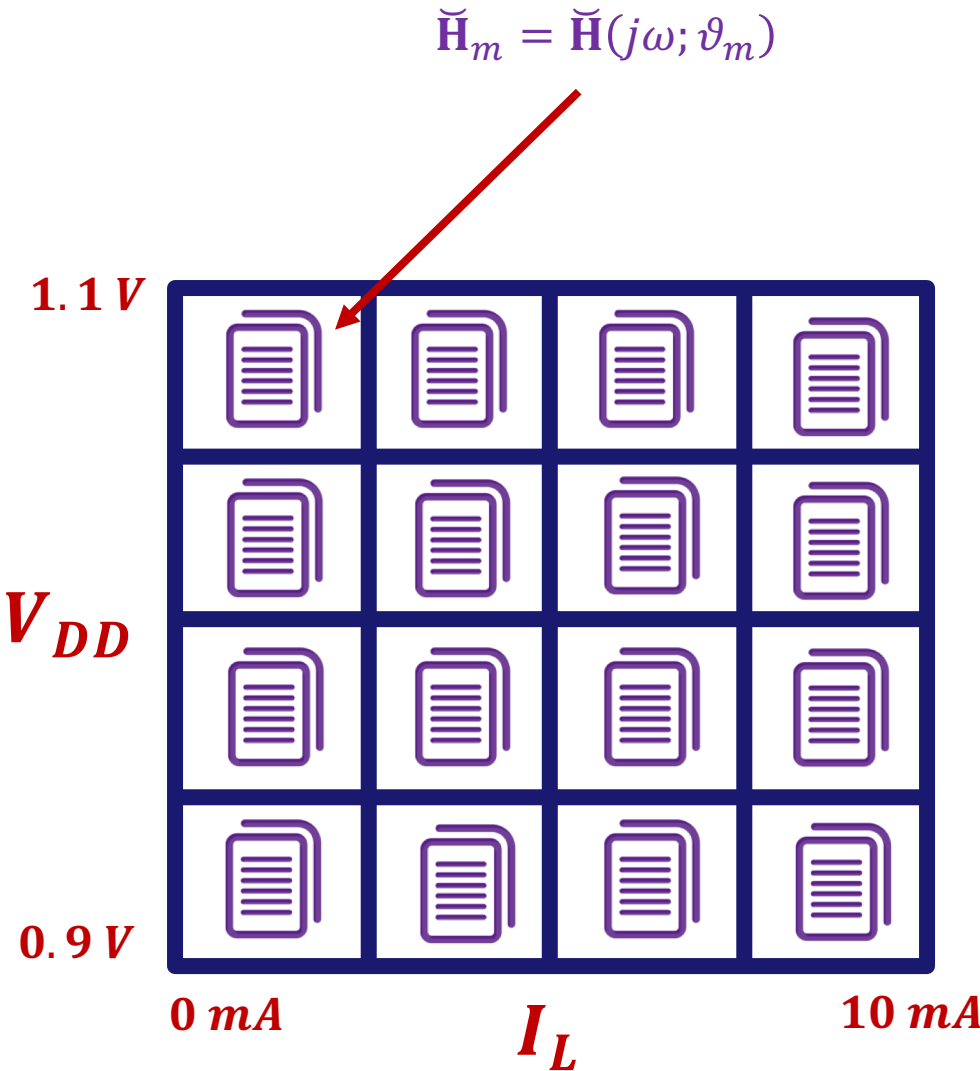
$$H(s; \vartheta) = \frac{N(s; \vartheta)}{D(s; \vartheta)}$$

Parameterized model



$$V_{DD} \in [0.9, 1.1] V \quad I_L \in [0, 10] mA$$

$$U_0 = \begin{bmatrix} V_{DD} \\ I_L \end{bmatrix} \text{ Induce the parameterization}$$

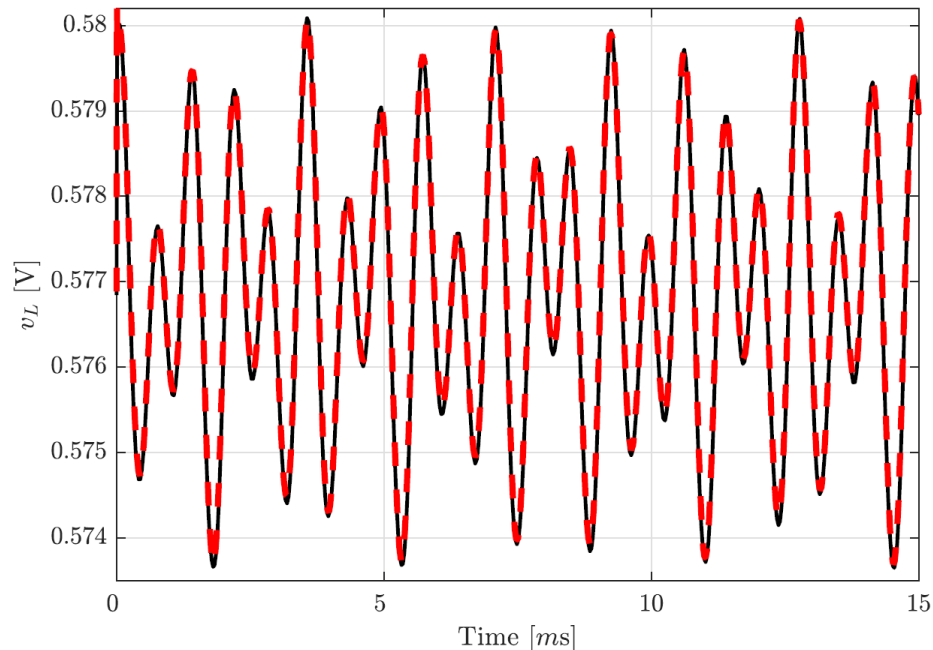


Bias point: $V_{DD} = 1V$, $I_L = 5mA$

Computed time span: $100ms$

Small-signal: multitone noise of amplitude $120mV$ superimposed to V_{DD}

Regulated Voltage



Dashed Red Lines : Model

Black lines: post layout LDO

Model time requirements: 363 ms

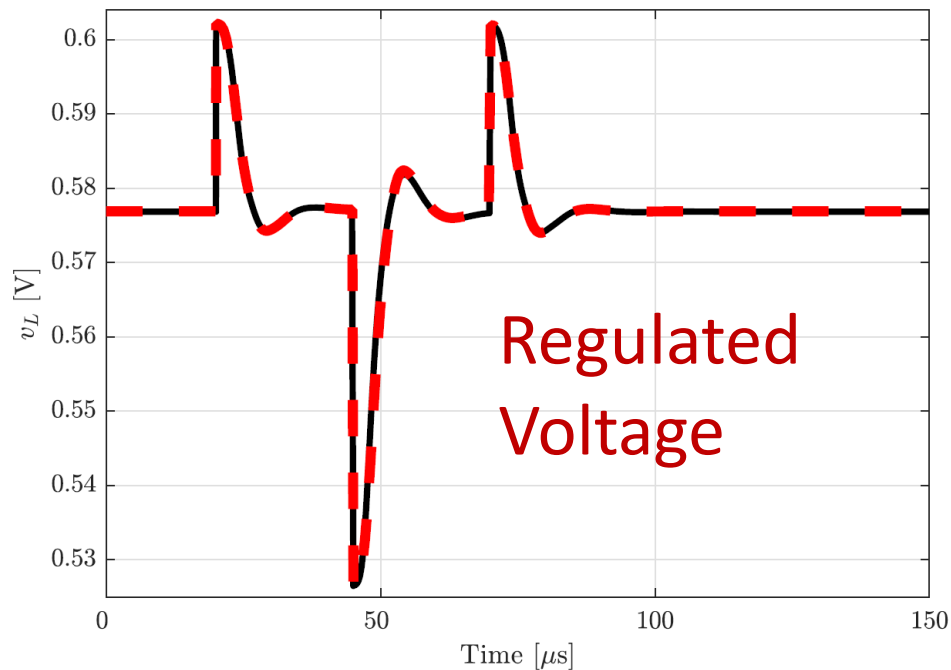
Transistor level post Layout: 258 s

SPEED UP FACTOR: 700X

Bias point: $V_{DD} = 1V$, $I_L = 5mA$

Computed time span: $100\mu s$

Small-signal: Sequential square pulses of amplitude $\pm 25mV$ over V_{DD}



Dashed Red Lines : Model
Black lines: post layout LDO

Model time requirements: 93 ms

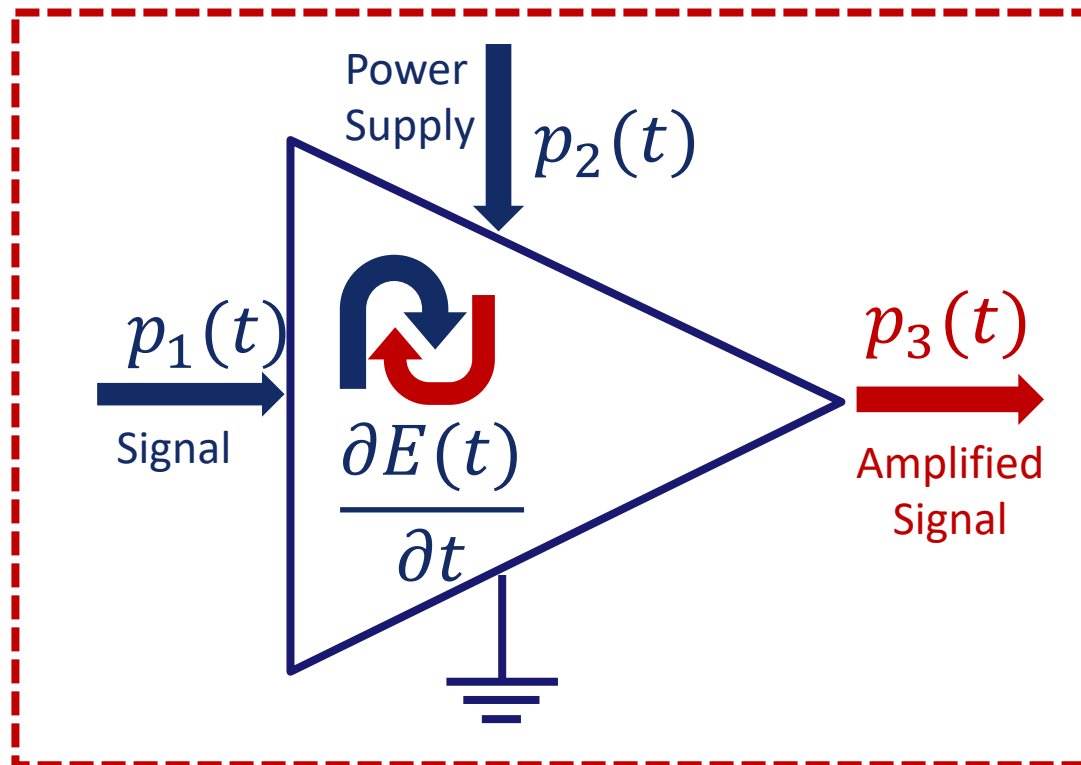
Transistor level post Layout: 63 s

SPEED UP FACTOR: 675X

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Any integrated circuit is not able to generate energy on its own
Proper circuit functioning is allowed by external power supply

Illustrative Example: 3-P Amplifier



The amplifier fulfills the **dissipation inequality**:

$$\frac{\partial E(t)}{\partial t} \leq p_1(t) + p_2(t) - p_3(t)$$

$E(t)$: Stored energy

$p_i(t)$: i -th power flow

Energetic constraints reflect into **NL dynamics** (e.g. saturation)

For linear affine systems we have:

$$p(t) = (U_0 + \tilde{u})^T (Y_0 + \tilde{y}) \quad \text{AND} \quad E(x) = \frac{1}{2} x^T P x + q^T x + c, \quad P = P^T$$

NEW RESULT: DISSIPATIVITY OF LINEAR AFFINE SYSTEMS

$$\exists P, q: \tilde{z}^T \Sigma(P) \tilde{z} + 2\theta_0(P, q, U_0, Y_0)^T \tilde{z} - 2U_0^T Y_0 \leq 0$$

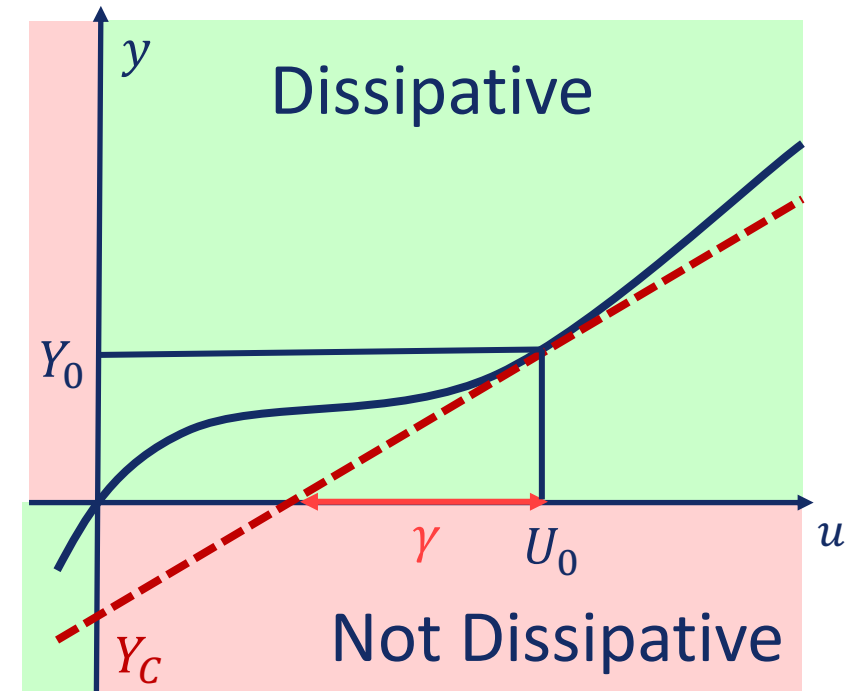
Additional terms due to different input power

$$p(t) = U_0^T Y_0 + U_0^T \tilde{y} + \tilde{u}^T Y_0 + \tilde{u}^T \tilde{y}$$

DC power: $U_0^T Y_0$ } **Positive**

Small signal power: $\tilde{u}^T \tilde{y}$ } **Undefined sign**

Cross-power: $U_0^T \tilde{y} + \tilde{u}^T Y_0$ } **Undefined sign**



- Recent advancements on macromodeling by Politecnico di Torino
 - **Macromodeling of large-scale systems (hundreds of I/O ports)**
 - Speaker: Marco De Stefano, PhD candidate
 - Compression strategies
 - Fast passivity verification and enforcement
 - **Parameterized (multivariate) macromodels**
 - Speaker: Alessandro Zanco, PhD candidate
 - Model structure and enhanced scalability (Radial Basis Functions – RBF)
 - Stability enforcement
 - **Small-signal modeling of (nonlinear) analog circuit blocks**
 - Speaker: Tommaso Bradde, PhD candidate
 - Embedding bias-dependence through parameterized macromodels
 - Theoretical assessment of dissipativity